

# Estimation of Media Volume Diameter from three Tropical Convective Systems using C-POL radar

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## Abstract

Since a differential reflectivity was proposed for rain estimation by Seliga and Bringi (1976), the polarimetric radar technique has attracted attention in radar meteorology. They showed that  $Z_{DR}$ , for an exponential rain drop size distribution (DSD), is directly related to the media volume diameter ( $D_0$ ). The algorithm described by Gorgucci et al. (2000) can essentially be applied for a gamma DSD, and generalized to account for raindrop oscillations of the linear axial ratio model of raindrop. In this paper we applied Gorgucci et al. (2000) algorithm to BMRC/C-POL radar to estimate  $D_0$ , and compared with surface disdrometer. This single point comparison shows that radar is under estimated than the disdrometer. Also the radar is under estimation the  $D_0$  sizes (slope 0.67), but the correlation coefficient is acceptable (0.84). It needs more research to overcome the problem of under estimation by C-Pol radar.

**Key word:** media volume diameter, C-POL

## 1. Introduction

Since a differential reflectivity was proposed for rain estimation by Seliga and Bringi (1976), the polarimetric radar technique has attracted attention in radar meteorology. They showed that  $Z_{DR}$ , for an exponential rain drop size distribution (DSD), is directly related to the media volume diameter ( $D_0$ ). Polarization parameters such as radar reflectivity ( $Z_H$ ), differential reflectivity ( $Z_{DR}$ ), linear reflectivity difference ( $Z_{DP}$ ), specific differential phase shift ( $K_{DP}$ ), linear depolarization ratio (LDR), as well as the correlation coefficient ( $\rho_{HV}$ ) have been successfully measured. These polarimetric measurements provide more information about precipitation and allow better characterization of hydrometeors. In general,  $Z_H$ ,  $Z_{DR}$ , and  $K_{DP}$  are used to estimate rain rate and drop spectrum, since they depend mainly on drop size and shape. Careful intercomparisons between radar measurements of  $Z_{DR}$  and  $D_0$  derived from surface disdrometers and airborne imaging probes have shown that  $D_0$  can be estimated to an accuracy of about 10-15% (Aydin et al., 1987; Goddard et al., 1982; Bringi et al., 1998).

A general gamma distribution model was suggested by Ulbrich (1983) to characterize the natural variation of the DSD. The specific differential propagation phase ( $K_{DP}$ ) is a forward scatter measurement whereas  $Z_{DR}$  is a backscatter measurement. The weighting of the DSD by  $Z_{DR}$  and  $K_{DP}$  is controlled by the variation of mean raindrop shape with size. A combination of the three radar measurements ( $Z_H$ ,  $Z_{DR}$  and  $K_{DP}$ ) can be utilized to estimate the DSD, specifically a parametric form of the DSD such as the

gamma DSD.

This paper presents the algorithms proposed by Gorgucci et al. (2000) for the estimation of  $D_0$  of a gamma DSD from polarimetric radar measurements at C-band frequency. Three cases of tropical convective system in Darwin Australia is tested. The  $D_0$  estimation from BMRC/C-POL radar is compared with the  $D_0$  derived from Joss and Waldvogel (1976) disdrometer on surface. The result shows that after attenuation and differential attenuation correction the C-band polarimetric radar can be used to estimate media volume diameter of gamma rain drop size distribution.

## 2. Raindrop size distribution data

Raindrop size distributions employed in this study were obtained from Joss and Waldvogel (1967) disdrometer data collected at Darwin, Australia during the period January – March 1999. Three convective system is selected to tested the  $D_0$  estimation by C-POL radar. The continental and monsoonal rainfall systems is described by Keenan and Carbone (1992).

Every 30 s the RD-69 disdrometer system recorded the number of raindrops in 20 size intervals or channels covering diameters in the range from 0.3 to 5.0 mm. System "dead" periods were corrected using the technique of Kinnell (1977). One-min DSD with  $R > 0.5$  mm h<sup>-1</sup> and containing more than 100 drops were considered for analysis. Distributions were discarded if zero counts in one or more consecutive channels were located between channels with nonzero counts. No correction for bin-sizing errors, as proposed by Sheppard (1990), was made. A gamma distribution of the form

$$N(D) = N_0 D^\mu \exp(-\Lambda D)$$

was fitted to the observed DSD, where  $N_0$  ( $\text{m}^{-3} \text{cm}^{-1\mu}$ ),  $\Lambda$  ( $\text{cm}^{-1}$ ), and  $\mu$  are the three DSD parameters. A maximum likelihood estimator (MLE) approach was employed to fit the gamma distribution. The fit procedure extended from the first channel recording nonzero counts to the largest channel recording nonzero counts ( $D_{\max}$ ). The incomplete gamma functions were solved explicitly employing the Van Wijngaarden–Dekker–Brent Method (Press et al. 1992), obviating the need to assume  $D_{\max}/D_0$  is large in the calculation of  $D_0$ .

### 3. $D_0$ estimation by C-Pol radar

Seliga and Bringi (1976) showed that for an exponential distribution, the two parameters of the DSD, namely  $N_w$  and  $D_0$ , can be estimated using  $Z_{DR}$  and  $Z_H$ . They used a two step procedure where they estimated  $D_0$  using an equilibrium raindrop shape model and subsequently used that in the expression for  $Z_H$  to estimate  $N_w$ . This procedure can essentially be applied for a gamma DSD, and generalized to account for raindrop oscillations using the linear model in the form

$$r = 1 - \beta D.$$

the  $r$  is axial ratio,  $D$  is equilibrium diameter of raindrop,  $\beta$  is a constant. Gorgucci et al. (2000) using simulations to derived an estimator for  $D_0$  as the following form,

$$\hat{D}_0 = a_1 Z_H^{b_1} (Z_{DR})^{c_1}$$

These coefficients for C-band are

$$a_1 = 0.59, \quad b_1 = 0.064, \quad c_1 = 0.024 \beta^{-1.42}$$

The procedure for estimating the gamma DSD parameters is as follows: First, correcting the attenuation and differential attenuation by the method of Bringi et al. (2001). Second, estimate  $\beta$  using the algorithm described by Gorgucci et al. (2000), and subsequently, estimate  $\hat{D}_0$ .

The radar data was collected from the Bureau of Meteorology Research Centre C-band (5.3 cm) dual-polarimetric radar (C-POL) which was located on Darwin Australia in 1999. For the C-POL radar specifications and definitions of all observed quantities, see Keenan et al. (1998). We focus on three tropical convective systems with heavy rain that occurred on 15 January, 1 and 17 March 1999.

### 4. results and conclusion

In order to evaluate the performance of the  $D_0$  estimation by using C-band polarimetric radar. We analysis three tropical convective systems passing through the D-scale rain gauge network settle on Darwin Australia. The  $D_0$  estimated by C-POL radar is compared with the  $D_0$  estimated from the surface disdrometer in the rain gauge network.

Figure 1 is the  $D_0$  space distribution estimated by C-Pol radar on 0600UTC 15 January 1999. The contour lines represent the radar reflectivity factor. The different

colors represent different  $D_0$  sizes which estimated by C-POL radar. The result show that most large  $D_0$  is in the front region of strong convection. This feature is same with the results by Maki et al. (2001). Which use the surface disdrometer data to analyze tropical continental squall line in Darwin, Australia.

Figure 2 shows the detail comparison of the disdrometer and radar estimated  $D_0$ . The radar data and disdrometer data is shifted in space and time lag by the help of surface rain gauge data. After the space and time lag shift adjustment the results improved greatly, the correlation coefficient increases from 0.71 to 0.84.

The  $D_0$  estimation by C-band polarimetric radar was tested, and compared with surface disdrometer. The method proposed by Gorgucci et al. (2000) is applied for BMRC/C-POL radar which under estimates the  $D_0$  sizes (slope 0.67), but the correlation coefficient is acceptable (correlation 0.84). It needs further research on the algorithm of  $D_0$  estimation for C-band polarimetric radar to overcome the under estimation problem.

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### Reference:

- Aydin, K., H. Direskeneli, and T. A. Seliga: Dual-polarization radar estimation of rainfall parameters compared with ground-based disdrometer measurements: 29 October 1982, Central Illinois experiment. *IEEE Trans. Geosci. Remote Sens.*, GE-25, 834–844, 1987.
- Bringi, V. N., V. Chandrasekar, and R. Xiao: Raindrop axis ratio and size distributions in Florida rainshafts: an assessment of multiparameter radar algorithms. *IEEE Trans. Geosci. Remote Sensing*, 36, 703–715, 1998.
- Bringi, V.N., T.D. Keenan and V. Chandrasekar, 2001a: Correcting C-band radar reflectivity and differential reflectivity data for rain attenuation: A self-consistent method with constraints, *IEEE Trans. Geosci. Remote Sens.*, vol. 39, 1906–1915.
- Gorgucci, E., G. Scarchilli, and V. Chandrasekar: Measurement of mean raindrop shape from polarimetric radar observations. *J. Atmos. Sci.*, 57, 3406–3413, 2000.
- Keenan, T. D., and R. E. Carbone, 1992: A preliminary morphology of precipitation systems in tropical northern Australia. *Quart. J. Roy. Meteor. Soc.*, 118, 283–326.
- Keenan, T. D., K. Glasson, F. Cummings, T. S. Bird, J. Keeler, and J. Lutz, 1998: The BMRC/NCAR C-band polarimetric (C-POL) radar system. *J. Atmos. Oceanic Technol.*, 15, 871–886.
- Kinnell, P. I. A., 1977: A preliminary report on the

commercial version of the Joss-Waldvogel rainfall distrometer. Division of Soils Divisional Rep. 21, Commonwealth Scientific and Industrial Research Organization, Canberra, ACT, Australia, 12 pp. [Available from CSIRO Land and Water, GPO Box 1666, Canberra, ACT 2601, Australia.]

Press, W. H., S. A. Teukolsky, W. Vetterling, and B. P. Fleming, 1992: Numerical Recipes in C: The Art of Scientific Computing. Cambridge University Press, 994 pp.

Seliga, T.A., and V.N. Bringi: Potential use of the radar

reflectivity at orthogonal polarizations for measuring precipitation. *J. Appl. Meteor.*, 15, 69–76, 1976.

Sheppard, B. E., 1990: Effect of irregularities in the diameter classification of raindrops by the Joss-Waldvogel disdrometer. *J. Atmos. Oceanic Technol.*, 7, 180–183.

Ulbrich, C. W.: Natural variations in the analytical form of raindrop size distributions. *J. Climate Appl. Meteor.*, 22, 1764–1775, 1983.

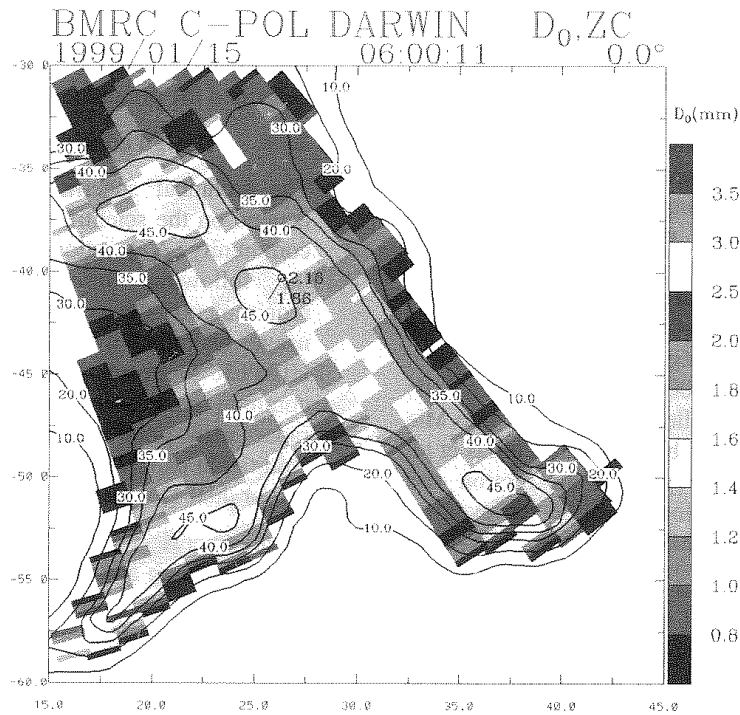


Fig 1 Space distribution of the  $D_0$  estimated by C-Pol radar.

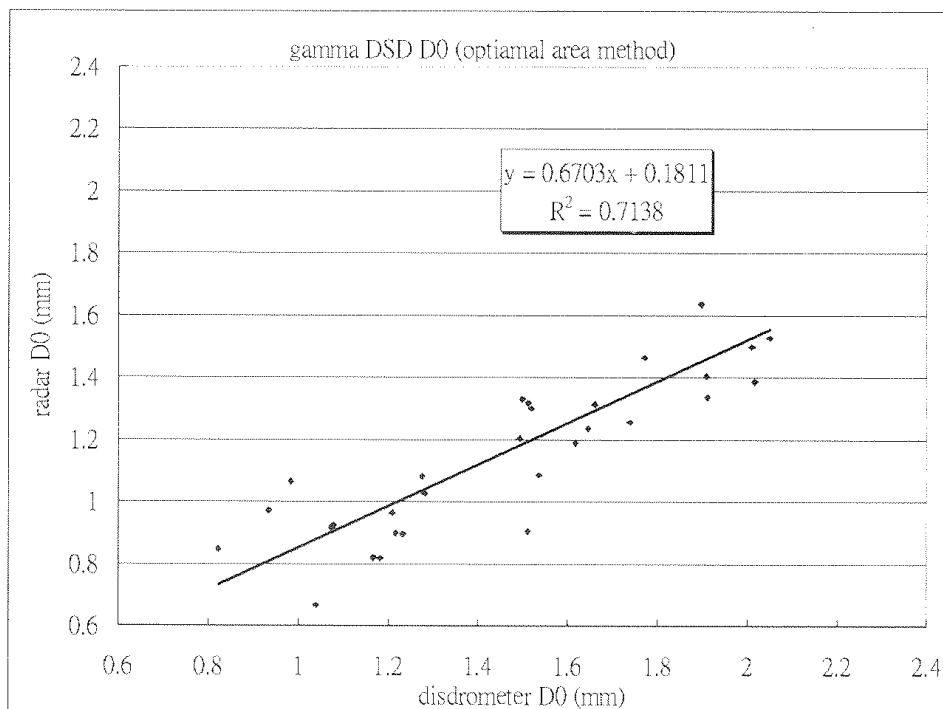


Fig 2 Scatter plot of the  $D_0$  estimated by C-POL radar and RD-69 disdrometer.